



Neutrino cross sections

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IceCube Detector



IceCube Simulation Chain



Neutrino Interactions

Charged Current

$$u_{\ell} + N \rightarrow \ell^{-} + X$$
 $\bar{\nu}_{\ell} + N \rightarrow \ell^{+} + X$

Neutral Current

$$u_{\ell} + N \rightarrow \nu_{\ell} + X$$
 $\bar{\nu}_{\ell} + N \rightarrow \bar{\nu}_{\ell} + X$

At relevant energies for IceCube the process of deep inelastic scattering is dominating (E > 5 GeV).

Deep Inelastic Scattering



DIS Kinematic Invariants

Bjorken scaling variable

$$x = \frac{Q^2}{2M\nu}$$

• Inelasticity in laboratory frame $y = \frac{\nu}{E}$

Four-momentum transfer

$$q = k_1 - k_2$$

 $Q^2 = -q^2 = -(k_1 - k_2)^2$

Inclusive Leading Order CC Cross Section

$$\frac{\mathrm{d}^2\sigma\left(\nu\mathbf{N},\bar{\nu}\mathbf{N}\right)}{\mathrm{d}x\mathrm{d}Q^2} = \frac{G_{\mathsf{F}}^2M_W^4}{4\pi(Q^2+M_W^2)^2x}\sigma_{\mathsf{r}}\left(\nu\mathbf{N},\bar{\nu}\mathbf{N}\right)$$

$$\begin{split} \sigma_{\rm r} \left(\nu {\sf N} \right) &= \left[{\sf Y}_+ {\sf F}_2^\nu(x,{\sf Q}^2) - y^2 {\sf F}_{\sf L}^\nu(x,{\sf Q}^2) + {\sf Y}_- x {\sf F}_3^\nu(x,{\sf Q}^2) \right] \\ \sigma_{\rm r} \left(\bar{\nu} {\sf N} \right) &= \left[{\sf Y}_+ {\sf F}_2^{\bar{\nu}}(x,{\sf Q}^2) - y^2 {\sf F}_{\sf L}^{\bar{\nu}}(x,{\sf Q}^2) - {\sf Y}_- x {\sf F}_3^{\bar{\nu}}(x,{\sf Q}^2) \right] \end{split}$$

with
$$Y_{\pm} = 1 \pm (1 - y)^2$$

 $F_2^{\nu,\bar{\nu}}(x, Q^2) = 2 \sum_{i=u,d,\dots} \left[xq(x, Q^2) + x\bar{q}(x, Q^2) \right]$
 $xF_3^{\nu,\bar{\nu}}(x, Q^2) = 2 \sum_{i=u,d,\dots} \left[xq(x, Q^2) - x\bar{q}(x, Q^2) \right]$

Parton Distribution Functions

- ▶ PDFs (e.g. in F₂, F₃, F_L) can be measured in accelerator experiments.
- Different experiments probe different kinematical regions.
- Extrapolate PDFs to regions of smaller x to describe the cross section at highest energies.





Currently Implemented Cross Section



Include Corrections

- Lepton masses
- Higher order QCD processes
- Nuclear effects
- Radiative corrections
- Target mass effects
- Heavy quark production



References

[1] http://2.bp.blogspot.com/_OmpmpuJV3hw/ TT8G7cqHlXI/AAAAAAAABE/SjblMYF4mpY/s1600/ IceCube-schema.jpg.

[2] F. Halzen und A.D. Martin. *Quarks and leptons: an introductory course in modern particle physics.* Wiley, 1984.

[3] P. Newman. "Deep Inelastic Scattering at the TeV Energy Scale and the LHeC Project". In: *Nucl.Phys.Proc.Suppl.* 191 (2009).

[4] Cooper-Sarkar, Amanda, Philipp Mertsch, and Subir Sarkar. "The high energy neutrino cross-section in the Standard Model and its uncertainty." Journal of High Energy Physics 2011.8 (2011).

Parton Distribution Functions

- Convolute NLO matrix element with PDFs to obtain cross section.
- Parametrize PDFs in x at a scale Q₀², which is large enough to apply perturbative QCD.
- ▶ PDFs at scales Q² > Q₀² can be calculated with the DGLAP equations.
- Predict PDF values at unmeasured values of x.
- Uncertainties naturally increase outside the fitted region.