



Bundesministerium
für Bildung
und Forschung



Measurement of Neutrino Oscillations with IceCube

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Deutsche
Forschungsgemeinschaft





Outline of Talk

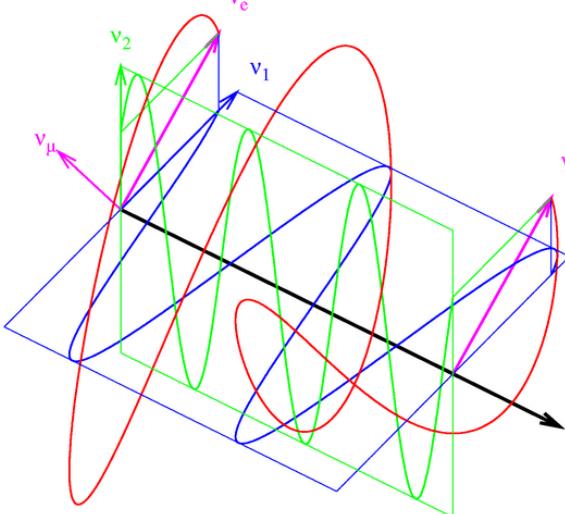
- **Introduction**
 - *What is neutrino oscillation?*
 - *What are atmospheric neutrinos?*
- **The IceCube Neutrino Observatory**
- **Idea of oscillation analyses**
 - *Energy and zenith observables*
 - *Log-likelihood test*
- **Current performance of IceCube analyses**
- **Improvements within my work**
 - *Dealing with low statistic Monte-Carlo simulations*
 - *Improving current reconstruction of observables*
 - *Neutrino flavor identification for multi-flavor analysis*
- **Summary and outlook**





Theory of Neutrino Oscillation

Three Generations of Matter (Fermions)			
	I	II	III
mass→	3 MeV	1.24 GeV	172.5 GeV
charge→	2/3	2/3	2/3
spin→	1/2	1/2	1/2
name→	u up	c charm	t top
Quarks	d down	s strange	b bottom
Leptons	v _e electron neutrino	v _μ muon neutrino	v _τ tau neutrino
Bosons (Forces)	Z ⁰ weak force		
	e electron	μ muon	τ tau
	W ⁺ weak force		



Why do neutrinos oscillate?

- Flavor eigenstates ($\nu_{e,\mu,\tau}$) do not match mass eigenstates of neutrinos ($\nu_{1,2,3}$):

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \cdot \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

- Pontecorvo-Maki-Nakagawa-Sakata Matrix U given by product of 3 $U(3)$ matrices:

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{U_{23}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{U_{13}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{U_{12}}$$

- Parameters: $s_{ij} = \sin(\theta_{ij})$ $c_{ij} = \cos(\theta_{ij})$ ($\delta = 0$)

called *mixing angles* (3 params.)



Theory of Neutrino Oscillation



Why do neutrinos oscillate?

$k=1,2,3$ E : neutrino energy
 $\alpha=e,\mu,\tau$ L : travelled distance
 Δm_{ij}^2 : squared mass diff. of states i & j

- Time expansion: $|\nu_k(t)\rangle = e^{-iE_k t} |\nu_k\rangle$

$$\rightarrow |\nu_\alpha(t)\rangle = \sum_{\beta=e,\mu,\tau} \left(\sum_k U_{\alpha k}^* e^{-iE_k t} U_{\beta k} \right) |\nu_\beta\rangle$$

- Likelihood for flavor change after distance $L=c \cdot t$:

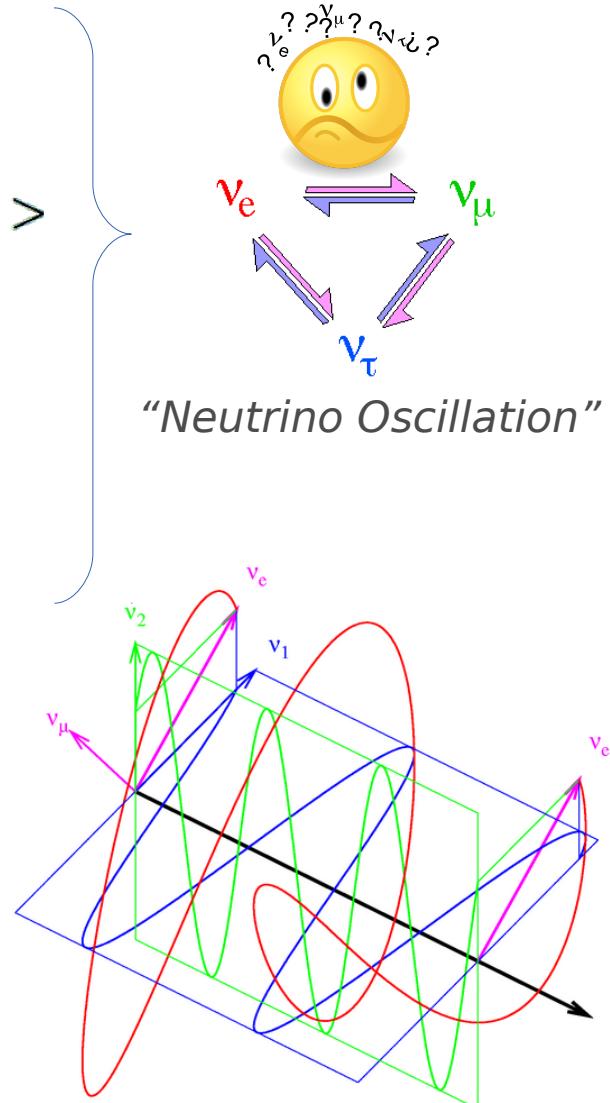
$$\rightarrow P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) = \sum_{k,j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* \exp\left(-i \frac{\Delta m_{kj}^2 L}{2E}\right)$$

- 5 oscillation parameters: $\theta_{12}, \theta_{23}, \theta_{13}, \Delta m_{12}^2, \Delta m_{32}^2$

- In simplified 2-flavor model:

$$P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

(in many cases sufficient to understand the dominant effects)





Theory of Neutrino Oscillation



Why do neutrinos oscillate?

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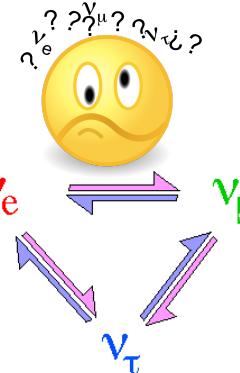
- Likelihood for flavor change after distance $L = c*t$:



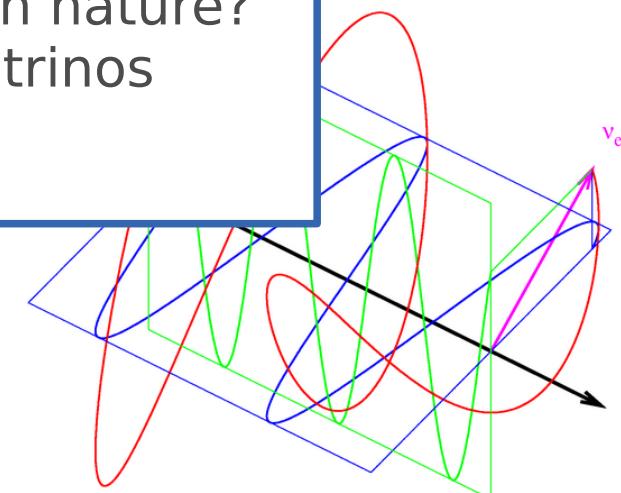
Ok, but where does this happen in nature?
Where can we get oscillating neutrinos from?

$$P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

(in many cases sufficient to understand the dominant effects)



"Neutrino Oscillation"





Atmospheric Neutrinos



Where do we get the neutrinos from?

- Primary cosmic rays interact with atmosphere
- Generate light mesons (pions, kaons)
- Decay of mesons results in neutrino production:

$$\pi^\pm \rightarrow \mu^\pm + \overset{(-)}{\nu_\mu} \rightarrow e^\pm + \overset{(-)}{\nu_e} + \nu_\mu + \bar{\nu}_\mu$$

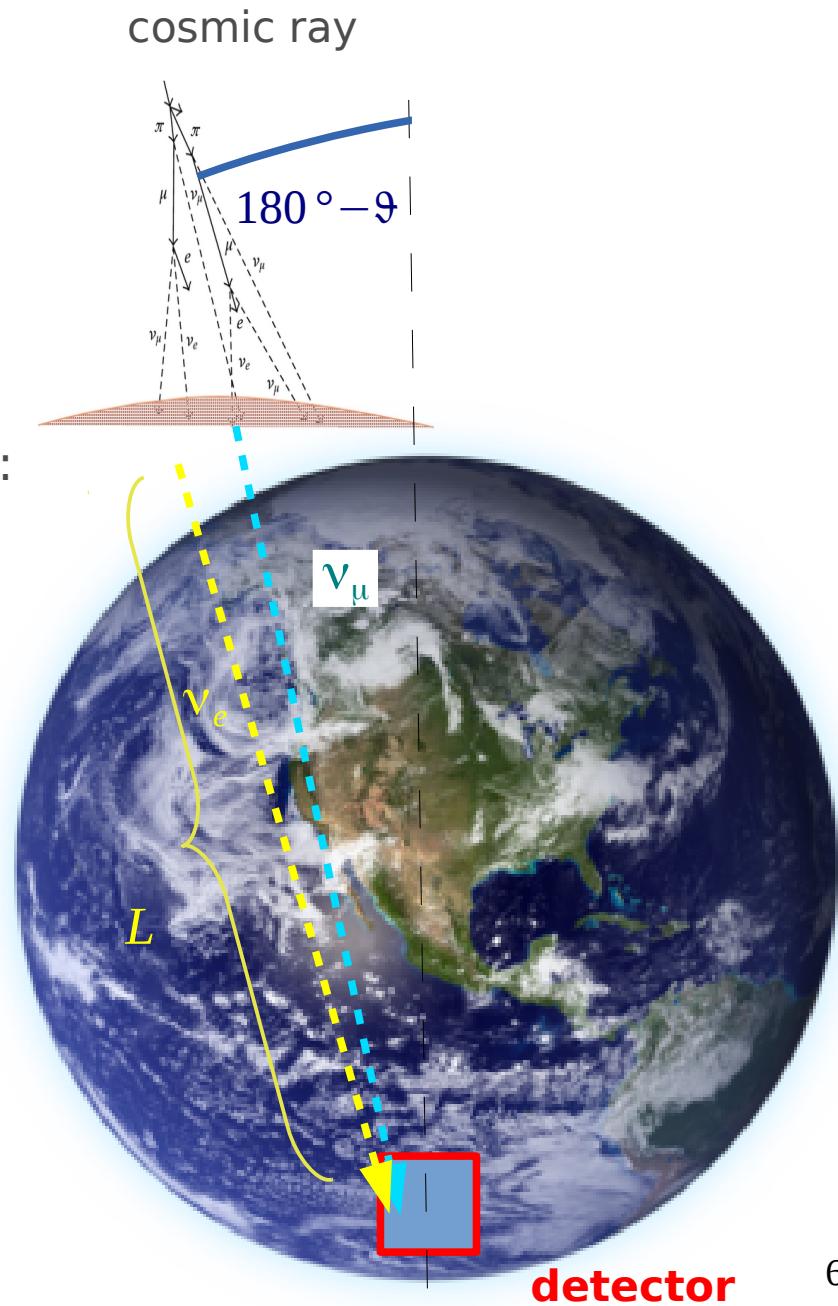
$$K^\pm \rightarrow \mu^\pm + \overset{(-)}{\nu_\mu} \rightarrow e^\pm + \overset{(-)}{\nu_e} + \nu_\mu + \bar{\nu}_\mu$$

- Derive distance L from zenith angle theta:

$$L \approx D \cdot \cos(\theta)$$

θ : zenith angle of incoming neutrino

D: diameter of Earth



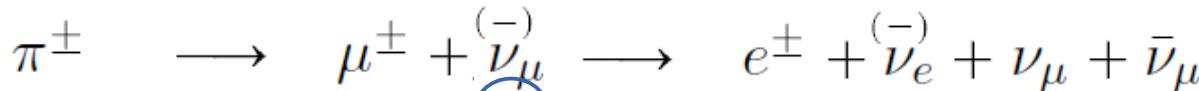


Atmospheric Neutrinos



Where do we get the neutrinos from?

- Primary cosmic rays interact with atmosphere
- Generate light mesons (pions, kaons)
- Decay of mesons results in neutrino production:



K^\pm



Do we have such a detector?

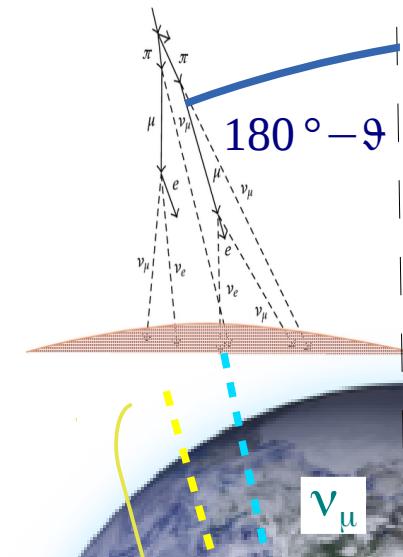
- Do

$$L \approx D \cdot \cos(\vartheta)$$

ϑ : zenith angle of incoming neutrino

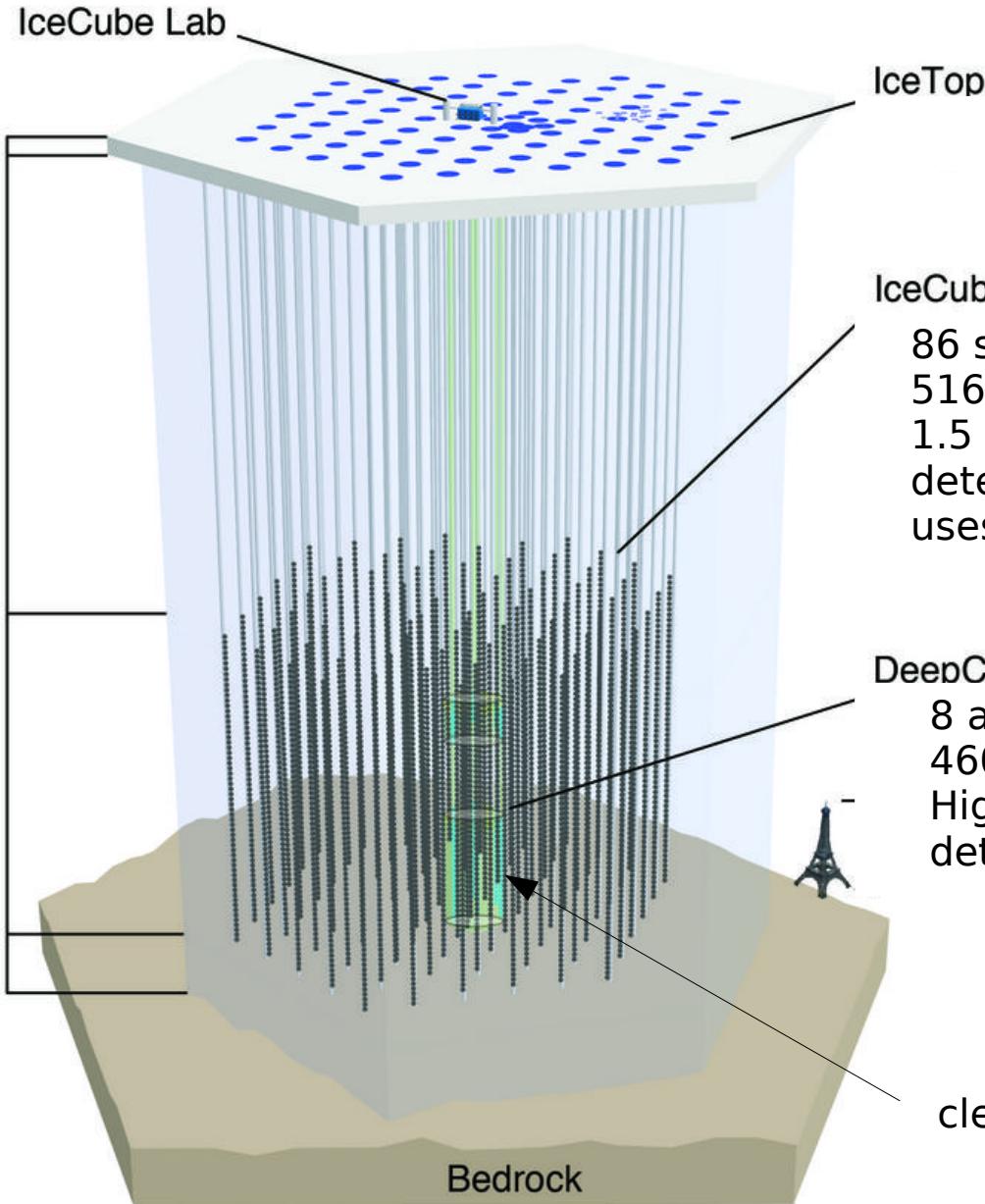
D : diameter of Earth

cosmic ray





IceCube Neutrino Observatory



IceCube Array

86 strings
5160 opt. sensors(DOMs)
1.5 - 2.5km depth
detects above $\sim 100\text{GeV}$
uses Cherenkov radiation

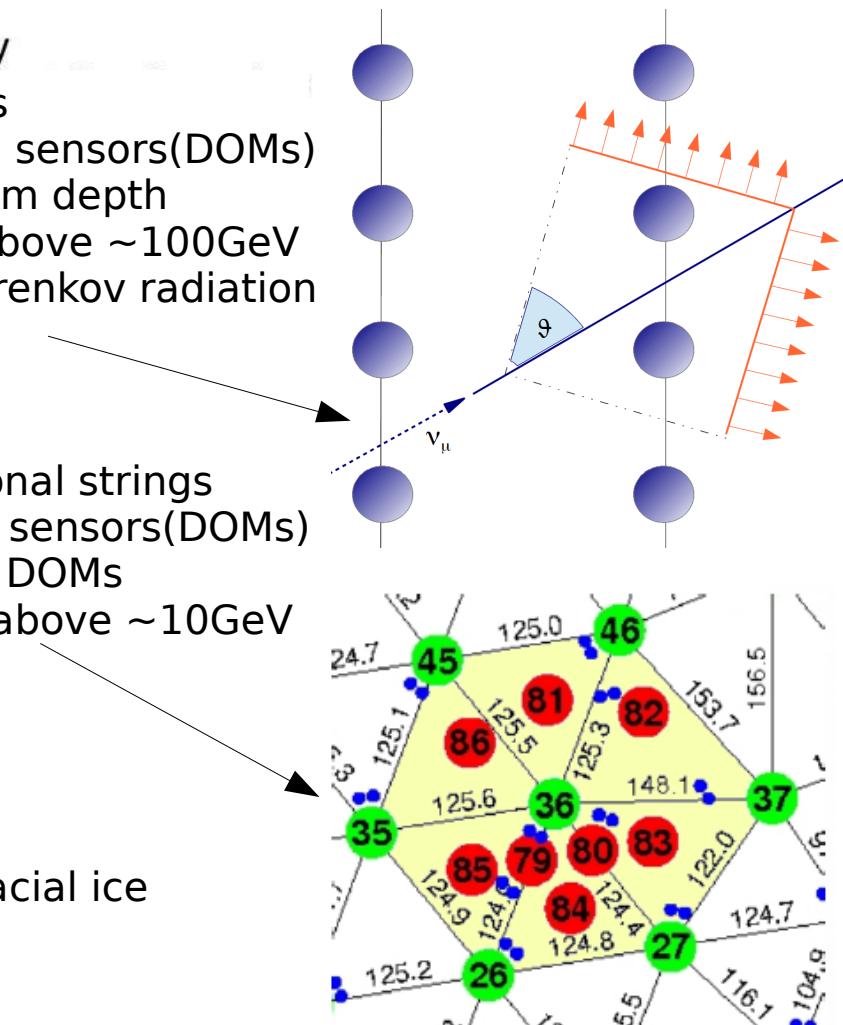
DeepCore

8 additional strings
460 opt. sensors(DOMs)
High-QE DOMs
detects above $\sim 10\text{GeV}$

clear glacial ice

What is IceCube?

At geographic South Pole,
finished 2010
 $\sim 1\text{km}^3$ neutrino detector





Idea of Oscillation Analyses



How can we measure the oscillation parameters?

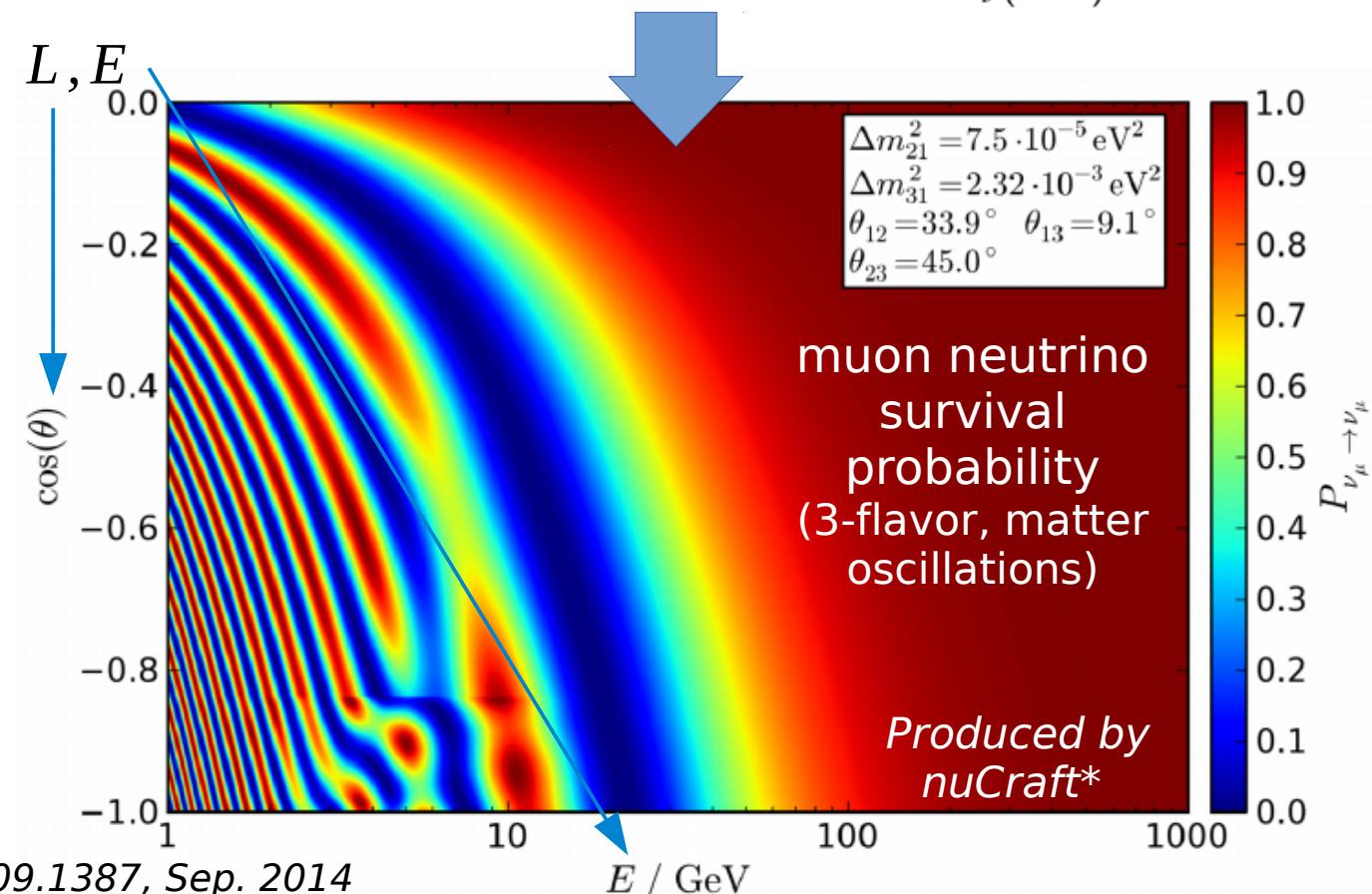
- Remember 2-flavor approximation: $P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$
- ν_μ -disappearance analysis:

$$\rightarrow P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta) \cdot \sin^2[1.27 \cdot \Delta m^2(\text{eV}^2) \frac{L(\text{km})}{E_\nu(\text{GeV})}]$$

- Two observables needed: L, E



Measure zenith angle and energy for each neutrino and apply log-likelihood analysis (LLH) to 2D histogram



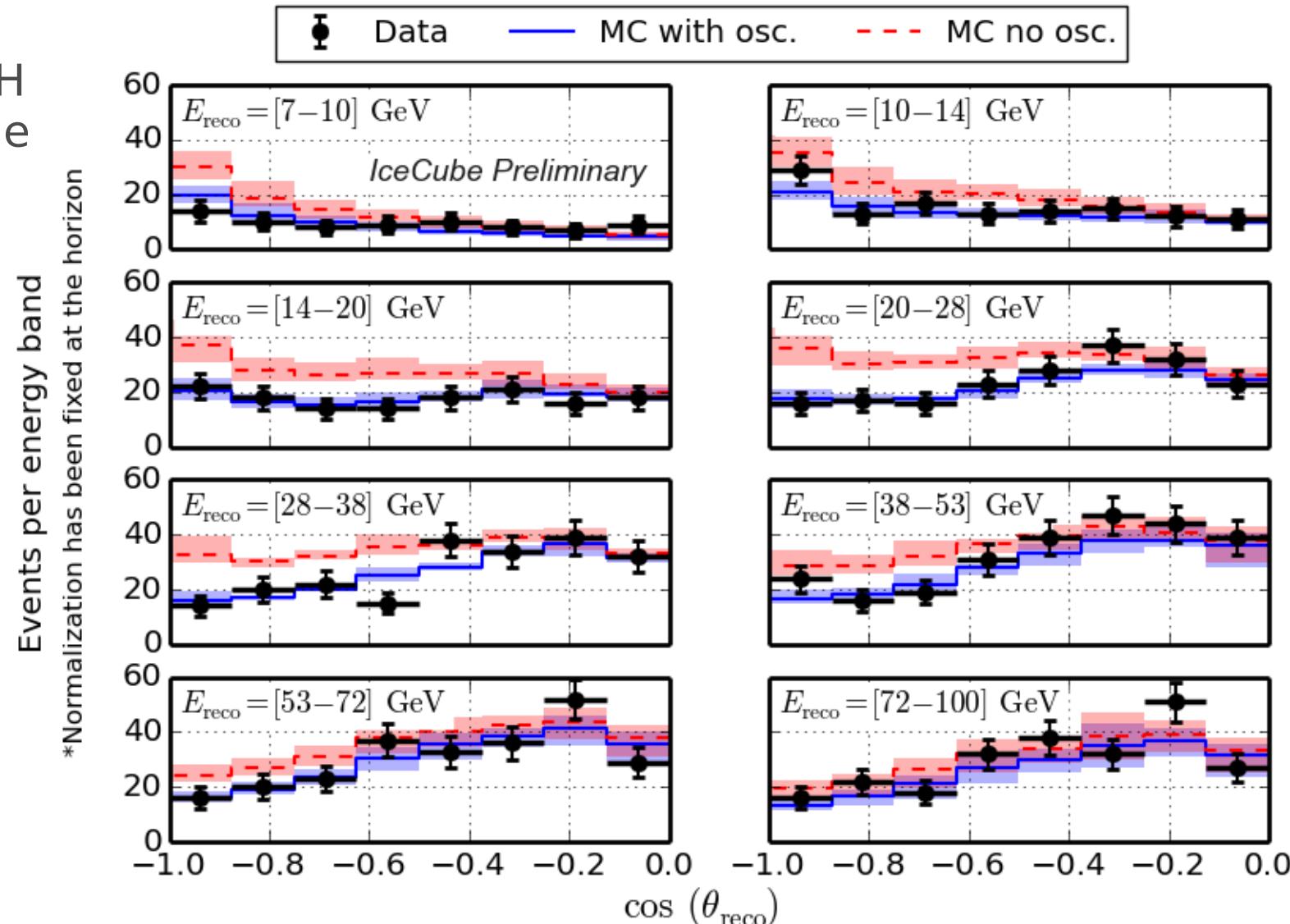


Current Status in IceCube

- Based on:

IceCube Collaboration, The measurement of neutrino oscillation with the full IceCube detector, ICRC 2013 Proceedings, arXiv:1309.7008

- **8x8 Bins** for LLH
- IC86 data sample
- High ν_μ -purity
- Contamination:
 - e-neutrinos
 - atm. muons
- Poissonian likelihood fct.
- Best fit(blue) vs null-hypothesis





Current Status in IceCube

- Based on:

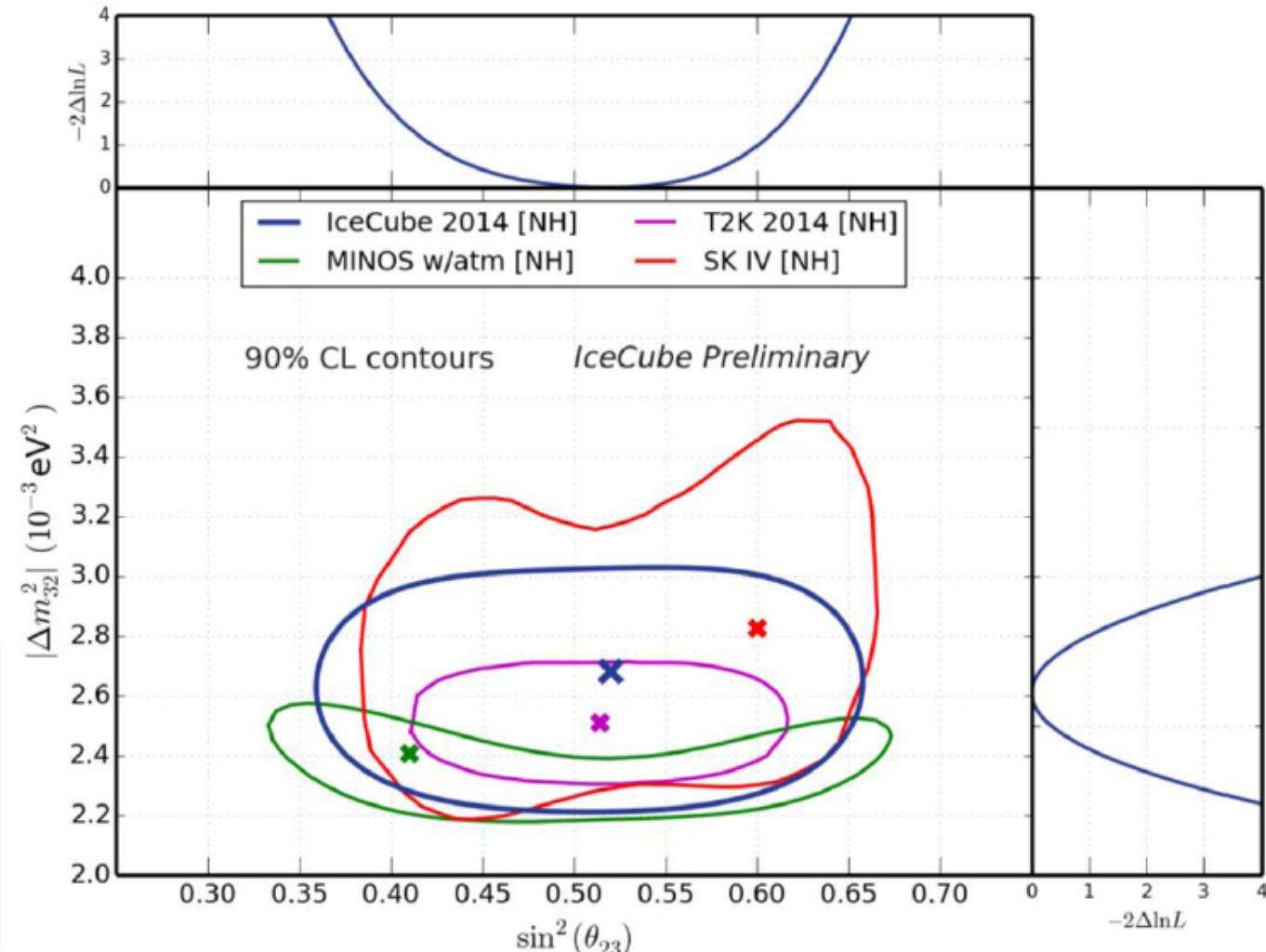
J.P. Yanez (IceCube Collaboration), Results from atmospheric neutrino oscillation with IceCube/DeepCore, Proceedings, Neutrino 2014, June 2014

- Fit of: $\Delta m_{32}^2, \theta_{23}$
- Other oscil. params. treated as nuisance parameters
- Competitive to world leading measurements

Best fit:

$$\Delta m_{23}^2 = (2.68 \pm 0.20) \cdot 10^{-3} \text{ eV}^2$$

$$\sin^2(\theta_{23}) = 0.51 \pm 0.09$$





Current Status in IceCube

- Based on:

J.P. Yanez (IceCube Collaboration), Results from atmospheric neutrino oscillation with IceCube/DeepCore, Proceedings, Neutrino 2014, June 2014

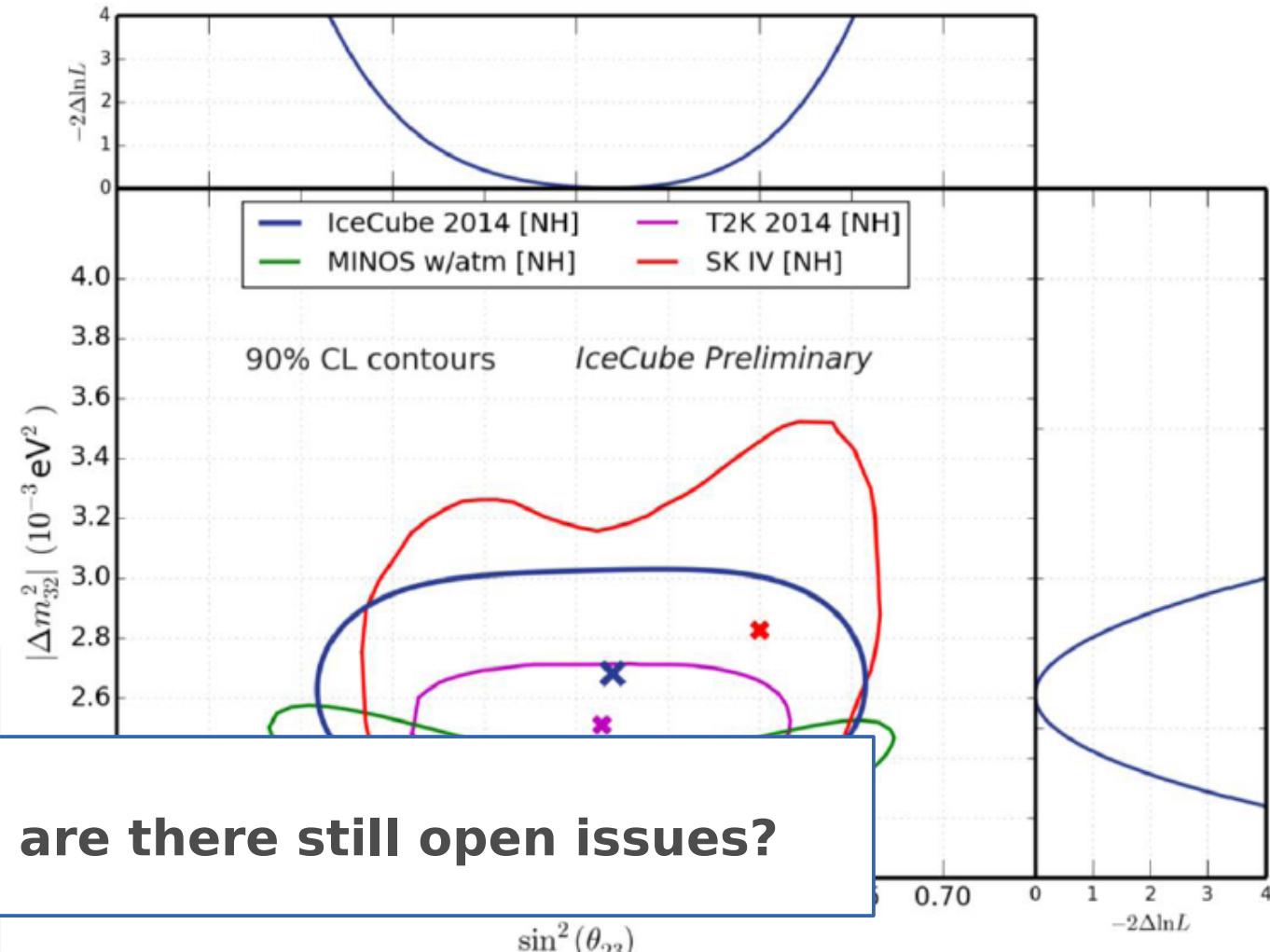
- Fit of: $\Delta m_{32}^2, \theta_{23}$
- Other oscil. params. treated as nuisance parameters
- Competitive to world leading measurements

Best fit:

$$\Delta m_{23}^2 = (2.68 \pm 0.08) \times 10^{-3} \text{ eV}^2$$
$$\sin^2(\theta_{23}) = 0.51 \pm 0.01$$



So, are there still open issues?





Improvements within my Work



So, are there still open issues?

- 1) Low Monte-Carlo statistics – how to deal with?
- 2) Reconstruction of low-energy events challenging



Improvements within my Work



So, are there still open issues?

- 1) Low Monte-Carlo statistics – how to deal with?
 → **Kernel Density Estimation (KDE)**
- 2) Reconstruction of low-energy events challenging

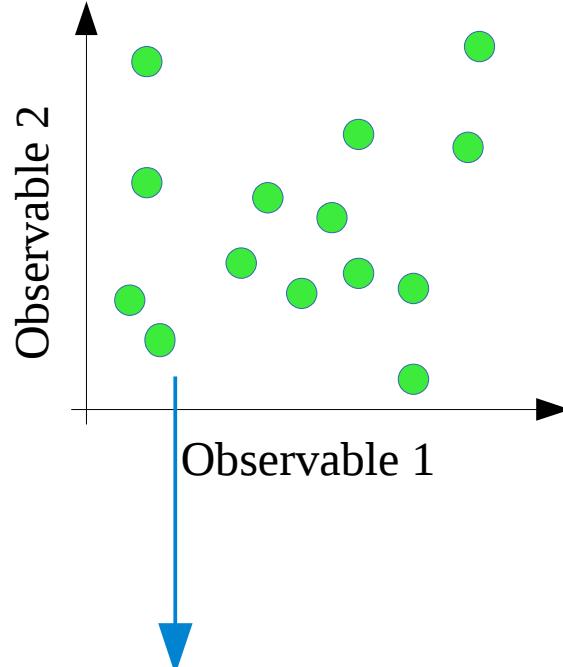


Idea of KDE

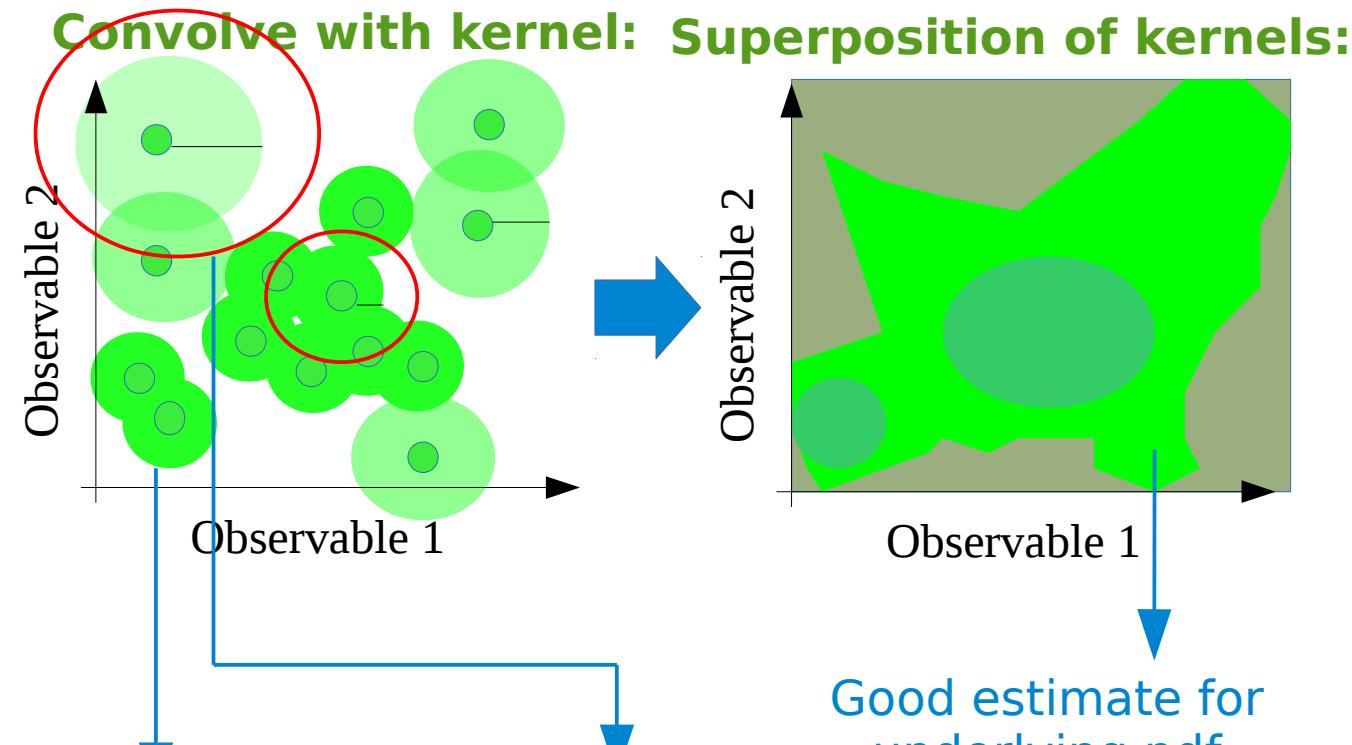


So, how can we deal with our limited knowledge of the pdf due to too low MC statistics?

Simulated events:



Insufficient MC statistic to estimate underlying pdf



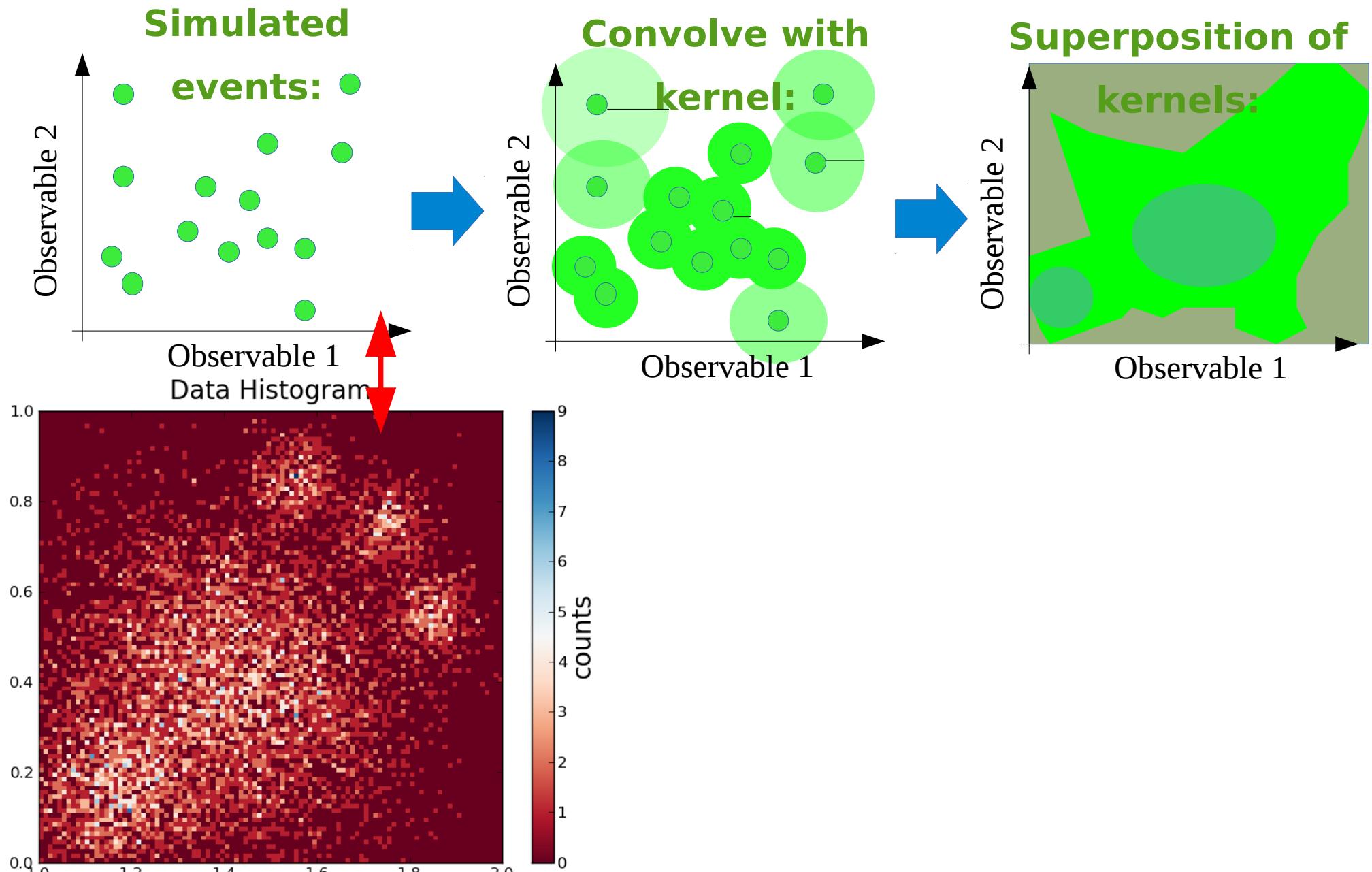
Convolve with Gaussian kernel

Width depends on statistic in neighbourhood

Good estimate for underlying pdf

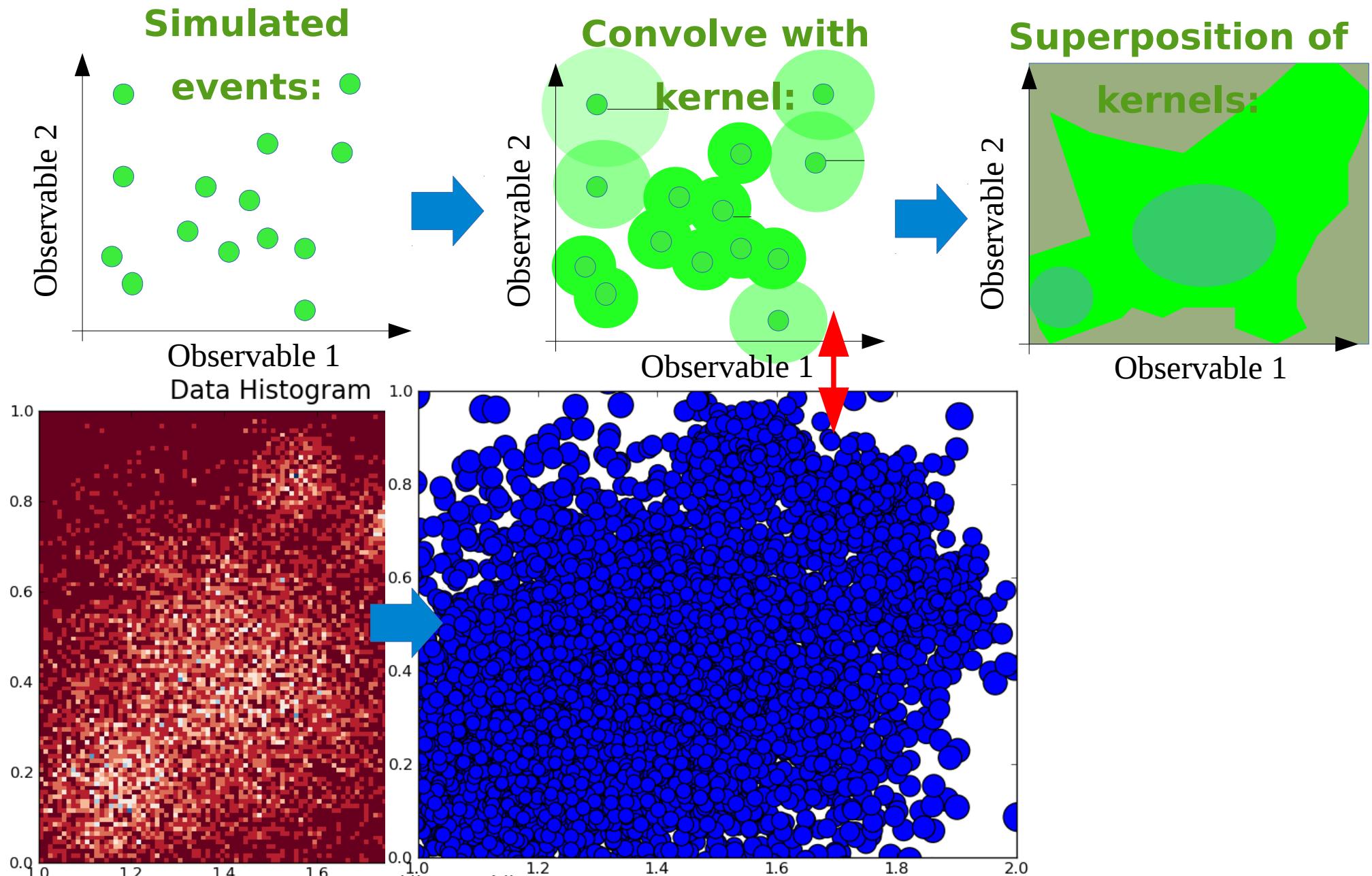


Reconstruction Performance





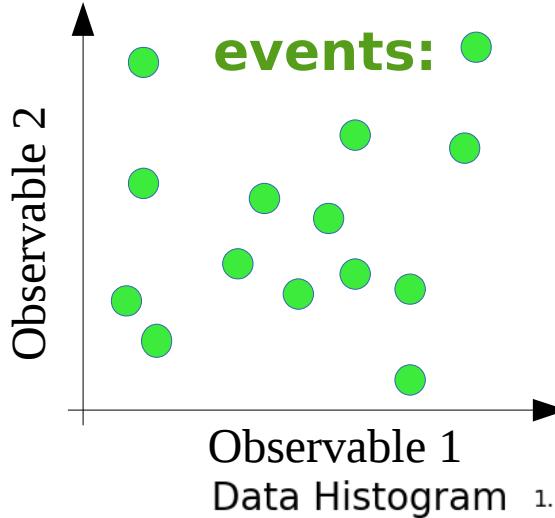
Reconstruction Performance



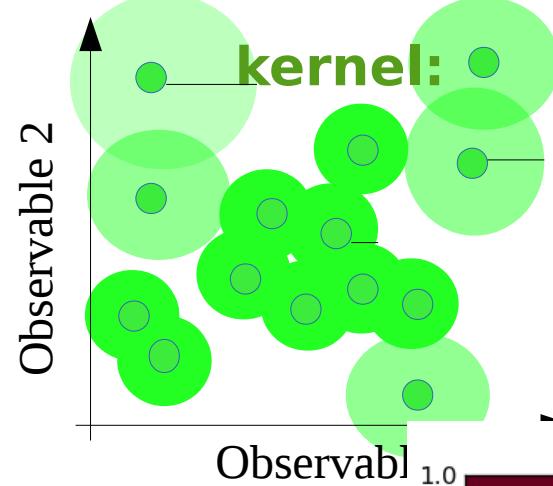


Reconstruction Performance

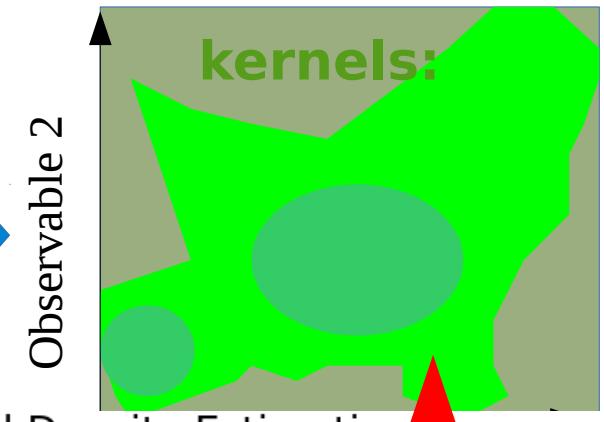
Simulated events:



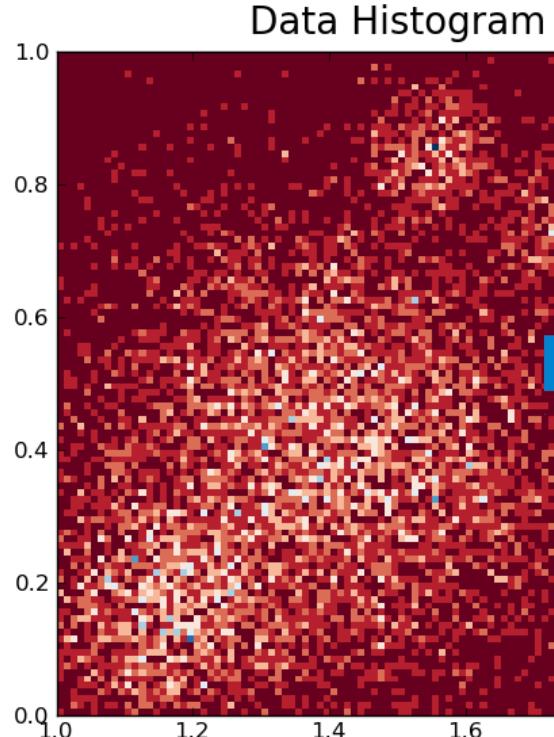
Convolve with kernel:



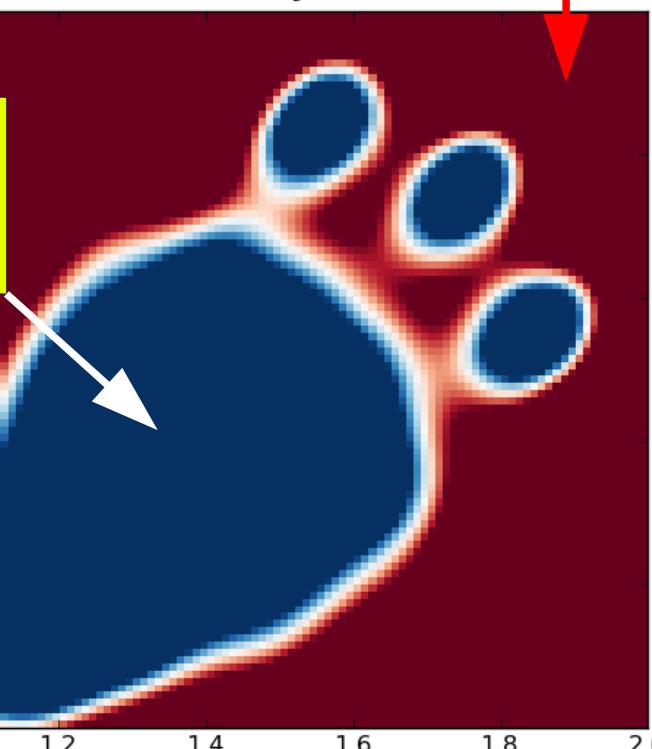
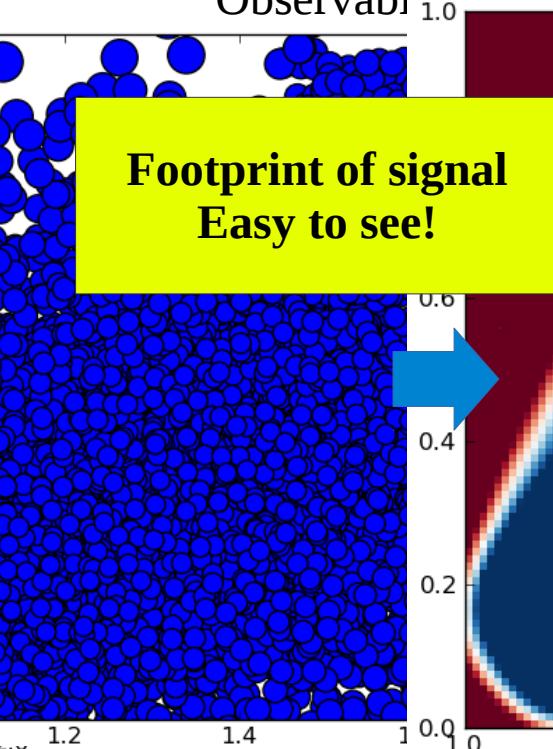
Superposition of kernels:



Data Histogram



**Footprint of signal
Easy to see!**





Improvements within my Work



So, are there still open issues?

1) Low Monte-Carlo statistics – how to deal with?

→ Kernel Density Estimation



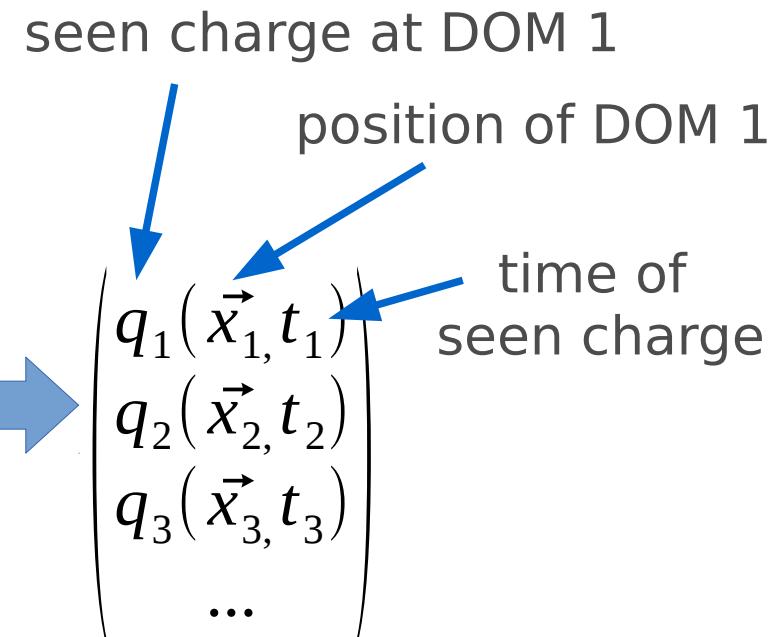
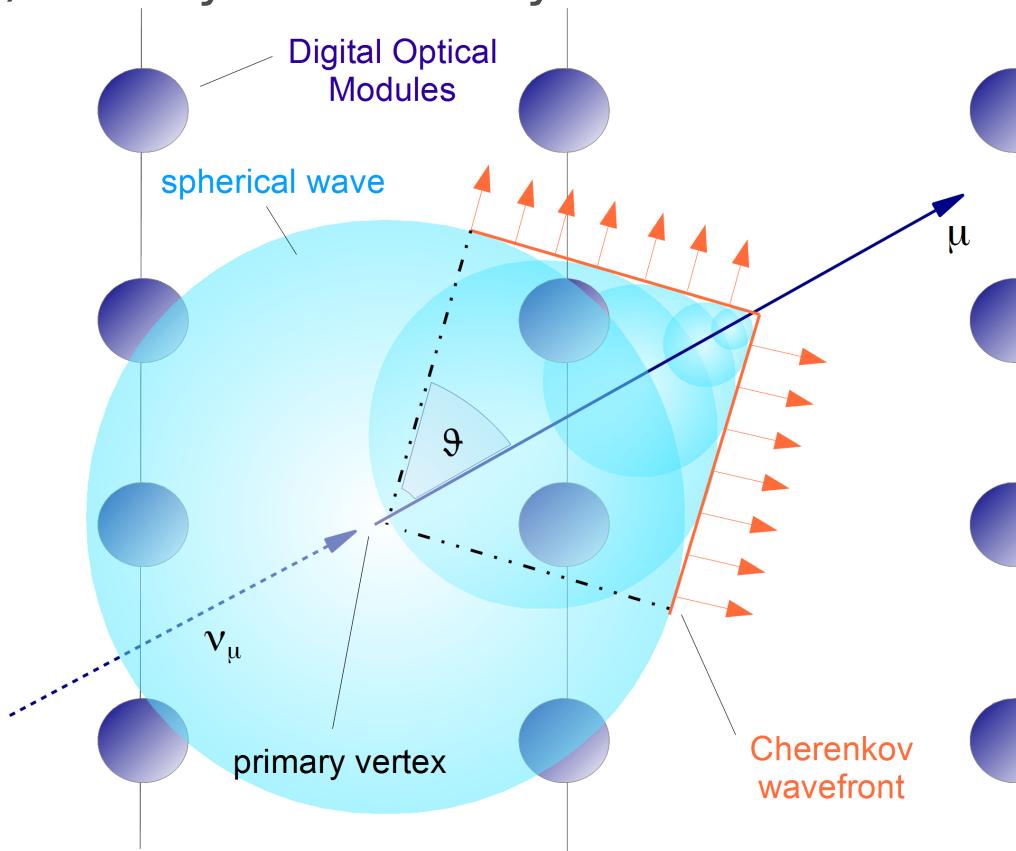
2) Reconstruction of low-energy events challenging

→ **Improved reconstruction algorithm**

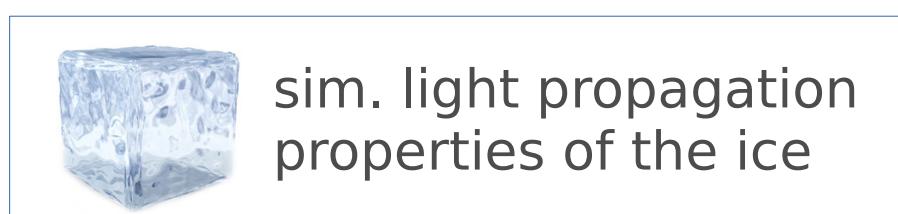


Idea of Current Recos.

1.) What you have in your data:



2.) What you know about the ice:



LLH of $E(\vec{y}_1)$ to cause $q(\vec{x}_1)$:

$$\Lambda(\vec{x}_1, \vec{y}_1, q(\vec{x}_1), E(\vec{y}_1))$$



Idea of Current Recos.

1.) special feature of LLH:

$$\Lambda(\vec{x}_1, \vec{y}_1, q(\vec{x}_1), E(\vec{y}_1)) \rightarrow q(\vec{x}_1) = \underbrace{\Lambda(\vec{x}_1, \vec{y}_1)}_{\text{<expected charge> at } x} \cdot \underbrace{E(\vec{y}_1)}_{\text{Caused by energy dep. at } y}$$

2.) For a given set of sources $\{(E_i, \vec{y}_i, t_i)\}$, we can rewrite this:

$$\begin{pmatrix} q_1(\vec{x}_1, t_1) \\ q_2(\vec{x}_2, t_2) \\ q_3(\vec{x}_3, t_3) \\ \dots \end{pmatrix} = \underbrace{\begin{pmatrix} \Lambda(\vec{x}_1, \vec{y}_1) & \Lambda(\vec{x}_1, \vec{y}_2) & \dots \\ \Lambda(\vec{x}_2, \vec{y}_1) & \Lambda(\vec{x}_2, \vec{y}_2) & \dots \\ \dots & \dots & \dots \end{pmatrix}}_{\Lambda: (\text{different for each set of Qs and Es})} \cdot \begin{pmatrix} E_1(\vec{y}_1, t_1) \\ E_2(\vec{y}_2, t_2) \\ E_3(\vec{y}_3, t_3) \\ \dots \end{pmatrix} \rightarrow \vec{Q} = \Lambda \cdot \vec{E}$$

\vec{Q} : (measurement)

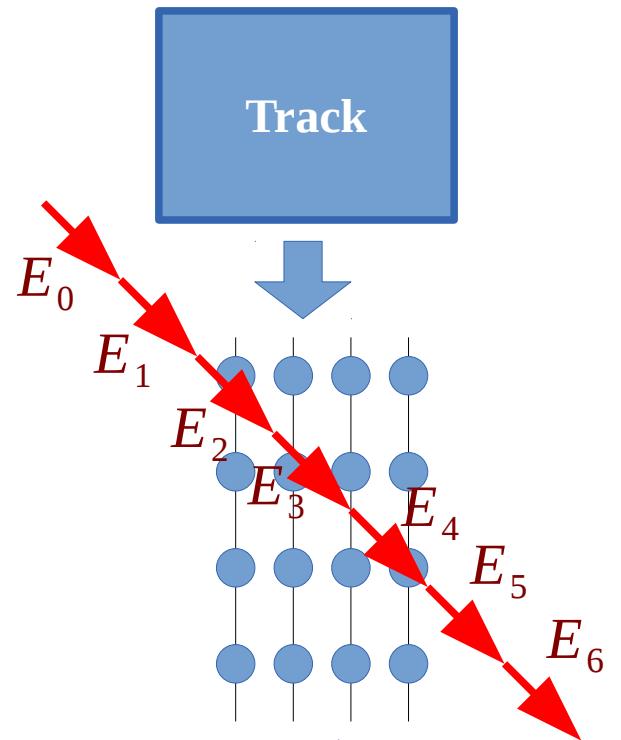
\vec{E} : (hypothesis)

$$\boxed{\rightarrow \vec{E} = \Lambda^{-1} \cdot \vec{Q}}$$

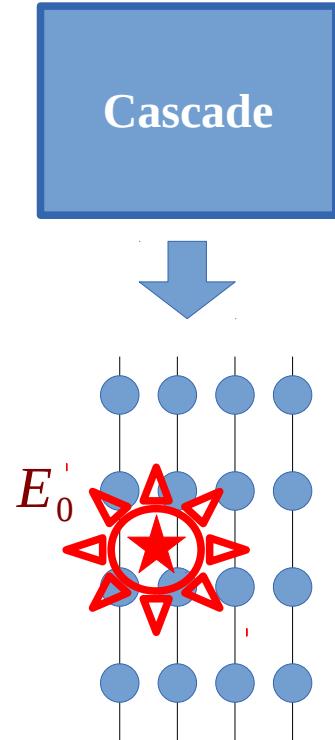


Existing Reconstructions

High-E muon-neutrino



NC or e-neutrino

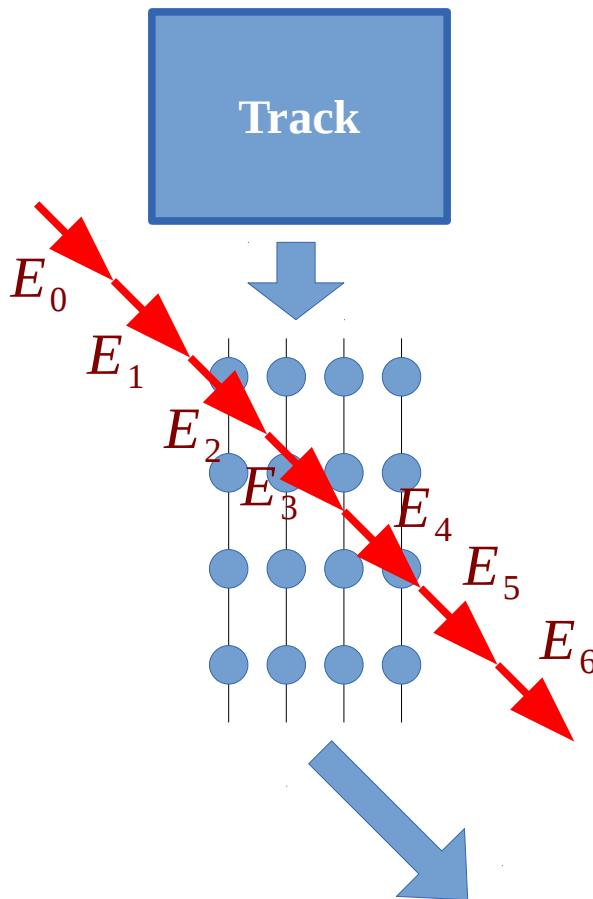


Energie calculation and LLH

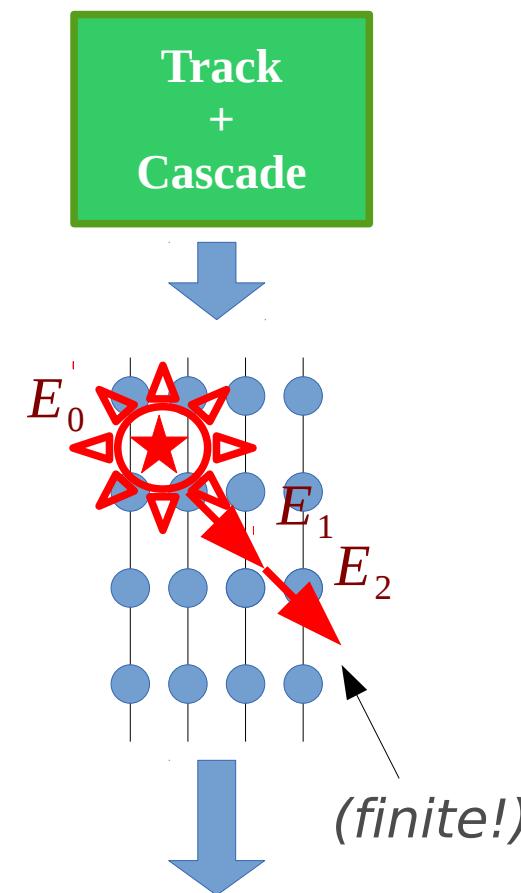


Existing Reconstructions

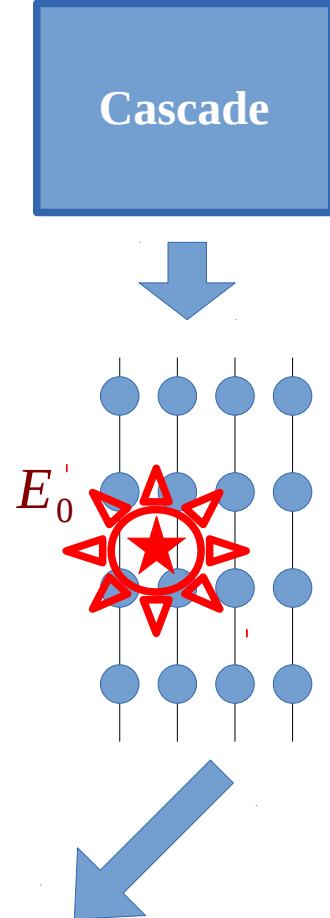
High-E muon-neutrino



Low-E muon-neutrinos:



NC or e-neutrino



Energie calculation and LLH



Improvements within my Work



So, are there still open issues?

1) Low Monte-Carlo statistics – how do deal with?

→ Kernel Density Estimation



2) Reconstruction of low-energy events challenging

→ Improved reconstruction algorithm





Summary

Summary:

- Neutrino oscillation of atmospheric neutrinos is measured by IceCube-DeepCore
- IceCube is/becomes competitive to world leading measurements (additional tau- and e-appearance analyses / sterile neutrinos, ...)
- Still space for improvements (**my work/outlook**):
 - Dealing with low statistics => K.D.E.
 - Improving reconstruction algorithms
 - Other ideas to be developed



References

Content references:

- IceCube Collaboration, The measurement of neutrino oscillation with the full IceCube detector, ICRC 2013 Proceedings, arXiv:1309.7008
Dmitry Chirkin, Likelihood description for comparing data with simulation of limited statistics, arXiv:1304.0735

Graphics references:

- <http://lappweb.in2p3.fr/neutrinos/neutimg/nkes/oscill.gif>
http://www.newworldencyclopedia.org/entry/Elementary_particle
<http://www.lead-conduct.de/wp-content/uploads/2012/05/Motivation-vs.-Desinteresse.png>
[http://commons.wikimedia.org/wiki/File:1_Earth_\(blank_2\).png](http://commons.wikimedia.org/wiki/File:1_Earth_(blank_2).png)

Thanks for listening



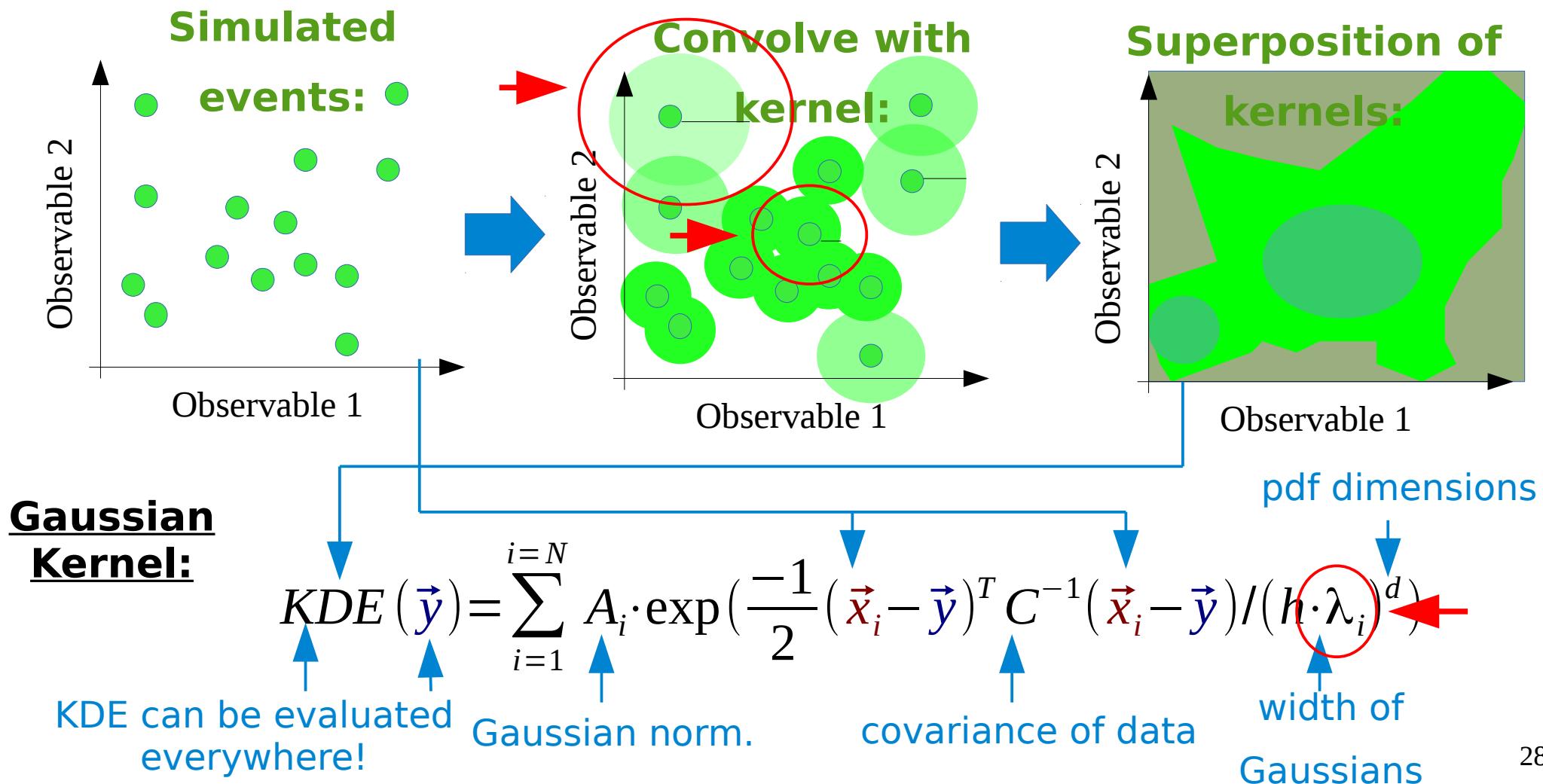
Backup



Idea of KDE



So, how can we deal with our limited knowledge of the pdf due to too low MC statistics?





Implementation of KDE

Gaussian Kernel:

$$KDE(\vec{y}) = \sum_{i=1}^N A_i \cdot \exp\left(-\frac{1}{2}(\vec{x}_i - \vec{y})^T C^{-1}(\vec{x}_i - \vec{y})/(h \cdot \lambda_i)^d\right)$$

KDE can be evaluated everywhere!

Gaussian norm.

pdf dimensions
↓
 $(h \cdot \lambda_i)^d$ ← width of Gaussians
↑ covariance of data

Seed bandwidth:

$$h = \left(\frac{N(d+2)}{4} \right)^{\frac{-1}{d+4}}$$

(„Silverman“ normalization)

Adaptive factor:

$$\lambda_i = \left(\frac{kde_i}{glob} \right)^{-\alpha}$$

$$glob = \exp\left(\frac{1}{N} \sum_{i=1}^N \ln(kde_i)\right)$$
$$kde_i = KDE(\vec{x}_i) \quad \Big|_{\lambda_i=1, \forall i}$$



What about simulations that require a weight to be introduced for every data point?



Implementation of KDE

Gaussian Kernel:

$$KDE(\vec{y}) = \sum_{i=1}^N w_i \cdot A_i \cdot \exp\left(-\frac{1}{2}(\vec{x}_i - \vec{y})^T C_w^{-1}(\vec{x}_i - \vec{y})/(h \cdot \lambda_i)^d\right)$$

KDE can be evaluated everywhere!

Gaussian norm.

covariance of data

pdf dimensions

width of Gaussians

Seed bandwidth:

$$h = \left(\frac{N(d+2)}{4} \right)^{\frac{-1}{d+4}}$$

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$$glob = \exp\left(\frac{1}{N} \sum_{i=1}^N \ln(kde_i)\right)$$

$$kde_i = KDE(\vec{x}_i) \Big|_{\lambda_i=1, w_i=1, \forall i}$$

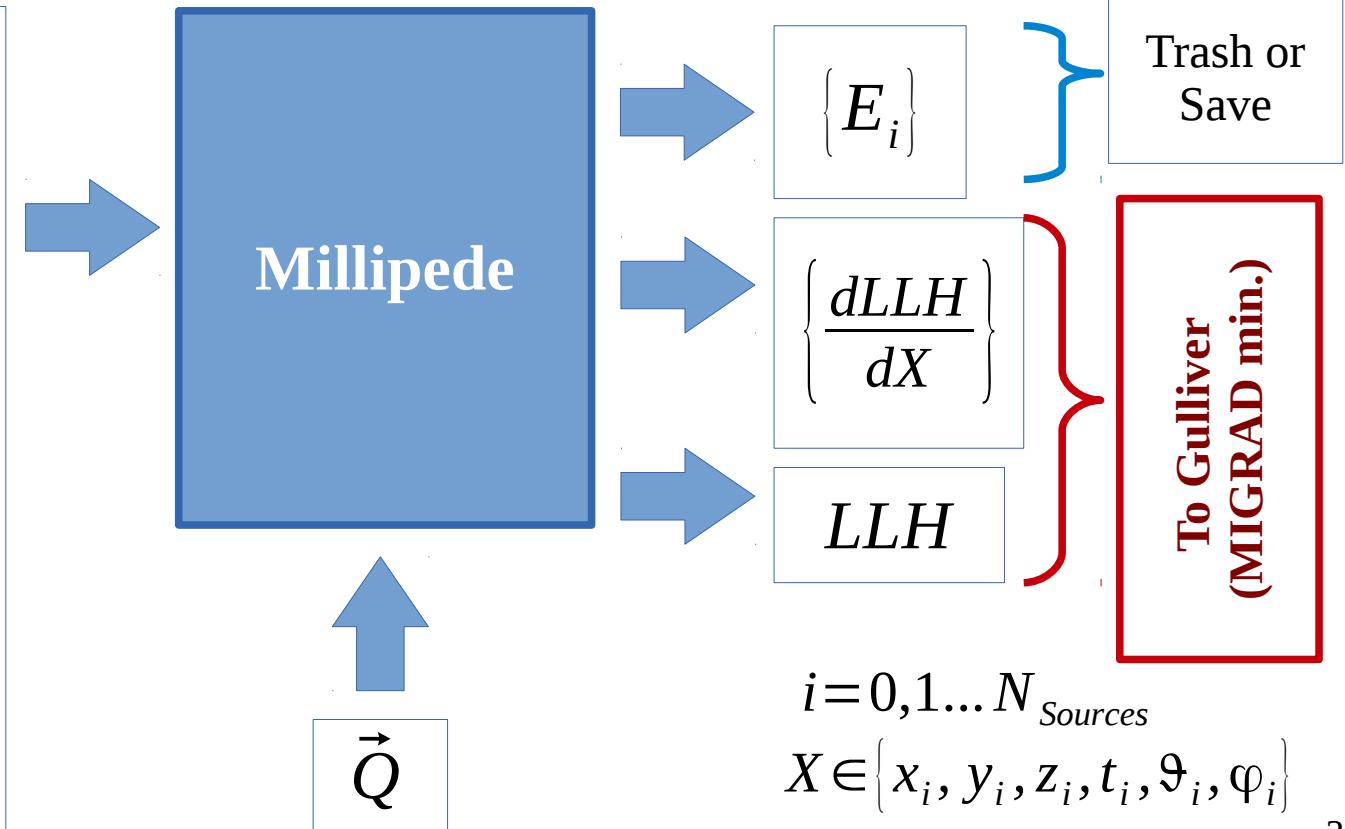
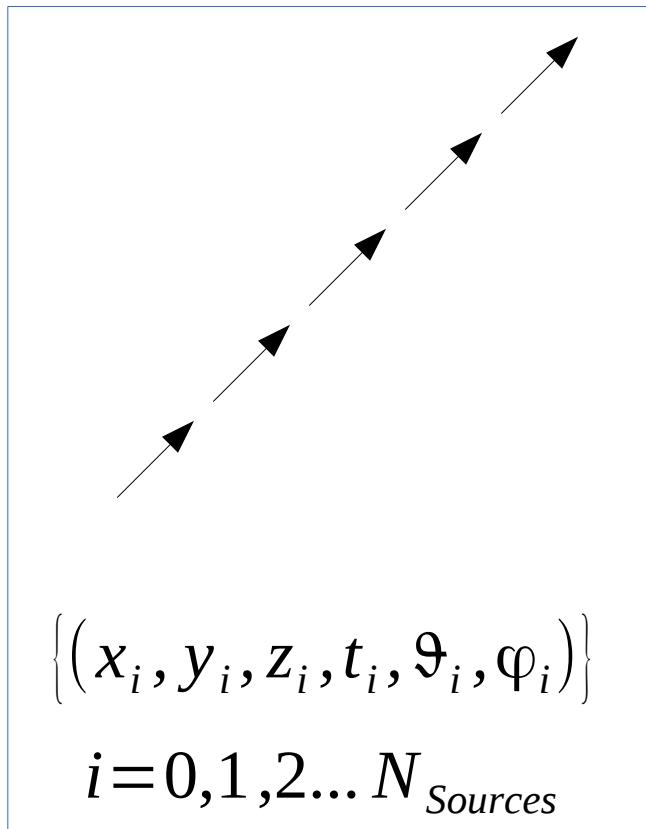
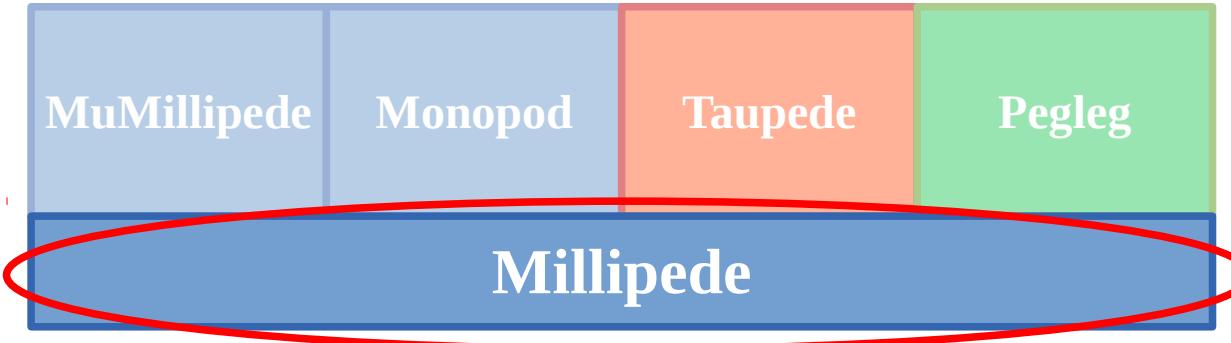


For more details on the method see:
[arXiv:0709.1616](https://arxiv.org/abs/0709.1616)



Millipede Introduction

So, what the key-element of all modules, “**Millipede**”, does is:





Pegleg

Hypothesis:
Cascade
+
FINITE track

